

DURATION OF BONDS

$\rightarrow IR \uparrow \rightarrow PV$
 $IR \downarrow \rightarrow PV$

INVERSE
RELATIONSHIP

\Rightarrow MEASURE OF IR SENSITIVITY

\Rightarrow MODIFIED DURATION

Ex. 2)

$$D = \sum_{t=1}^T t \times w_t$$

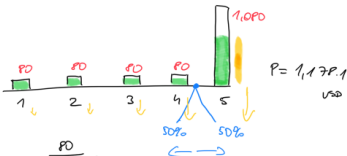
$$w_t = \frac{\frac{CF_t}{(1+IR)^t}}{PRICE}$$

FV = 1,000 USD

YTM = 4% \Rightarrow COUPON

CR = 8% \Rightarrow PD

TIME = 5 YEARS



$$w_1 = \frac{80}{(1.04)^1} \times \frac{1}{1,178.1}$$

$$w_2 = \frac{80}{(1.04)^2} \times \frac{1}{1,178.1}$$

\vdots

$$w_5 = \frac{1,080}{(1.04)^5} \times \frac{1}{1,178.1}$$

$$D = (1 \times w_1) + (2 \times w_2) + (3 \times w_3) + (4 \times w_4) + (5 \times w_5)$$

$$D = 4.37 \text{ YEARS}$$

$$MD = \frac{D}{1+IR} = \frac{4.37}{1.04} = 4.2\%$$

IR \uparrow 1% \Rightarrow PRICE \downarrow 4.2%

Ex. 3)

FACTORS INFLUENCE SENSITIVITY (DURATION)

- TTM \oplus
- COUPON \ominus
- YTM \ominus

INVESTMENT

RISK $\left\{ \begin{array}{l} \text{SYSTEMATIC} \rightarrow \text{BETA} \\ \text{NON-SYSTEMATIC} \end{array} \right.$

\rightarrow ELIMINATION BY DIVERSIFICATION

Ex. 1) CAPM $E_{Ri} = R_F + \beta_i \times (E_{Rn} - R_F)$

Labels: R_F (RISK FREE), β_i (RISK), $(E_{Rn} - R_F)$ (MARKET RISK PREMIUM)

\rightarrow WE DON'T KNOW

$$RRR = \frac{E_{Ri} - R_F}{\beta_i}$$

Ex. 2) $E_R = 8 + 0.7 \times (16 - 8) = 13.6\%$

Label: 5.6% (under 0.7)

| | | | | |
|--------|---|------------|---------------------------|--|
| Ex. 3) | 0 | -2,000,000 | | |
| | 1 | +600,000 | $\frac{600,000}{(1.1)^1}$ | $\left\{ \begin{array}{l} CF_t \\ (1+IR)^t \end{array} \right.$ |
| | 2 | +600,000 | $\frac{600,000}{(1.1)^2}$ | |
| | 3 | +600,000 | $\frac{600,000}{(1.1)^3}$ | |
| | 4 | +400,000 | $\frac{400,000}{(1.1)^4}$ | |
| | 5 | +400,000 | $\frac{400,000}{(1.1)^5}$ | |
| | 6 | +400,000 | $\frac{400,000}{(1.1)^6}$ | |
| | | | | $\begin{array}{r} 2,239,475.7 \\ - 2,000,000 \\ \hline 239,475.7 \\ \hline \text{NPV} \end{array}$ |

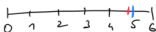
NPV = ?

IRR = ? $IRR > WACC$

10%

PP = 3.5 YEARS

DPP = 4.94 YEARS



MONEY MARKET HEDGE

Ex. 5)

FUTURE CASH OUTFLOW \rightarrow 1,000,000 USD ; 2 MONTHS
 FUTURE CASH INFLOW \rightarrow 1,000,000 USD ; 2 MONTHS

③ $\frac{1,000,000 \text{ USD}}{(1 + \frac{0.03}{6})} = 995,025 \text{ USD}$ (LEND)

② $\frac{995,025}{1.2500} = 796,020 \text{ EUR}$ (EXCHANGE)

① $796,020 \times (1 + \frac{0.04}{6}) = 801,327 \text{ EUR}$ (BORROW) (COST)

FUTURE CASH INFLOW \rightarrow 1,000,000 USD ; 2 MONTHS
 FUTURE CASH OUTFLOW \rightarrow 1,000,000 USD ; 2 MONTHS

③ $\frac{1,000,000 \text{ USD}}{(1 + \frac{0.03}{6})} = 995,025 \text{ USD}$ (BORROW)

② $\frac{995,025}{1.2500} = 796,020 \text{ EUR}$ (WE HAVE)